

Delay and Energy Efficiency Tradeoffs for Data Collections and Aggregation in Large Scale Wireless Sensor Networks

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Abstract—In this paper, we study efficient data collection for wireless sensor networks. We present efficient distributed algorithms with approximately the minimum delay, or the minimum messages to be sent by all nodes, or the minimum total energy consumed by all nodes. We analytically proved that all our methods are either optimum or are within constants factor of the optimum. We then investigate the possibility of designing one universal method such that the delay, the messages sent by all nodes, and the total energy costs by all nodes are all optimum or are within constants factor of optimum. Given a method \mathcal{A} for data collection, let ϱ_T , ϱ_M , and ϱ_E be the approximation ratio of \mathcal{A} in terms of time complexity, message complexity, and energy complexity respectively. We then show that, for data collection, there are networks of n nodes and maximum degree Δ , such that $\varrho_M \varrho_E = \Omega(\Delta)$ for any algorithm. We also prove that our method achieves the best tradeoffs in terms of the time complexity, message complexity and the energy complexity.

Index Terms—Time complexity, message complexity, energy, sensor networks, data collection, distributed algorithms.

I. INTRODUCTION

Wireless sensor networks (WSNs) have drawn considerable amount of research interests recently because they can collect the data, monitor the environment in a more efficient and convenient way. To design and deploy successful wireless sensor networks, a number of issues must be resolved such as deployment strategies, energy conservation, routing in dynamic environment, localization and so on. For wireless sensor networks, often the ultimate goal is to collect the data (either the raw data or in-network-processed data or both) from a set of targeted wireless sensors to some sink nodes and then perform some further analysis at sink nodes. Convergecast is the common many-to-one communication pattern used for these sensor network applications. In this paper, we study some fundamental complexity problems for data collection in wireless sensor networks.

Given a set U of wireless sensor nodes distributed in a two dimensional or three dimensional space, assume that a subset $V \subseteq U$ of nodes produced some data. *Data collection* is to collect the set of data items A_i stored in each individual node $v_i \in V$ to the sink node v_0 . We will first design efficient algorithms whose complexity is asymptotically same as (or

within a certain factor of) the complexity of the optimum for data collection. We will then study various complexity tradeoffs and show that our method achieves the asymptotically optimum complexity tradeoffs. The complexity of a problem is defined as the worst case¹ cost (time, message or energy) by the best algorithm. Studying the complexity of a problem is often challenging. Data collection and aggregation has been extensively studied in the community of networking and database. Surprisingly, little is known about the complexity tradeoffs of this operation.

In [12], five distributive aggregations *max*, *min*, *count*, *sum* and *average* are carried out efficiently on a spanning tree. Subsequent work did not quite settle the time complexity, the message complexity and the energy complexity of data collection and aggregation, nor the tradeoffs among these three possibly conflicting objectives. The closest results are [9]–[11]. All assume a complete wireless network, which is usually not true in practice. Furthermore, to the best of our knowledge, no fundamental results on the tradeoffs among the time complexity, message complexity, and energy complexity were known before this work.

To the best of our knowledge, we are the first to study the tradeoffs among the message complexity, time complexity, and energy complexity for data collection; we are the first to present lower bounds (and matching upper-bounds for some cases) on the message complexity, time complexity, and energy complexity for data collection in wireless networks. The main contributions of this paper are as follows.

We design algorithms whose time complexity and message complexity are within constant factors of the optimum. The minimum energy data collection can be done using minimum cost shortest path tree. We further show that no data collection algorithm can achieve approximation ratio ϱ_M for message complexity and ϱ_E for energy complexity with $\varrho_M \cdot \varrho_E = o(\Delta)$. We then prove that our data collection algorithm has energy cost within a factor $O(\Delta)$ of the optimum while its time and message complexity are within $O(1)$ of the corresponding optimum. Thus, our method achieves the best tradeoffs among the time complexity, message complexity and energy complexity.

The rest of the paper is organized as follows. In Section II, we first present our wireless sensor network model, define the problems to be studied in this paper, and then briefly review

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¹The worst case is to consider all networks of n nodes (and possibly diameter D , and maximum nodal degree Δ) and all possible distributions of all data items A over all nodes V .

the connected dominating set. We present several efficient methods for data collection in Section IV and we study the complexity tradeoffs of distributed data collection in Section V. Data aggregation is studied in Section VI. We review the related works in Section VII and conclude the paper in Section VIII.

II. PRELIMINARIES

A. Network Model

In this paper, we mainly focus on the complexities of data collection in wireless sensor networks. Thus, for simplicity, we assume a simple and yet general enough wireless sensor network model that is widely used in the community. We assume that there are $M + 1$ wireless sensor nodes $U = \{u_0, u_1, u_2, \dots, u_M\}$ that are deployed in a certain geographic region, where u_0 is the sink node. Each wireless sensor node corresponds to a vertex in a graph G and two vertices are connected iff their corresponding sensor nodes can communicate directly. The graph G is called the communication graph of this sensor network. We assume that links are “reliable”: when a node v_i sends some data to a neighboring node v_j , the total message cost is only 1, although in practice node v_i may need re-transmit several times. In some of the results, we further assume that all sensor nodes have a communication range r and a fixed interference range $R = \Theta(r)$. For simplicity, we may assume that $r = 1$, *i.e.*, the transmission range is normalized to one unit. In other words, the communication graph G is a *Unit Disk Graph* (UDG). Here a graph G is a unit disk graph if we have a one-to-one mapping from its vertices to 2-dimensional points such that there is an edge uv iff the Euclidean distance between the mapped points u and v is at most one unit.

Let $h(v_i, v_j)$ be the hop number of the minimum hop path connecting v_i and v_j in graph G , and $D(G)$ be the diameter of the graph, *i.e.*, $D(G) = \max_{v_i, v_j} h(v_i, v_j)$. Here, we assume that $D(G) \geq 2$. If $D(G) = 1$, then the graph G is simply a completed graph and all questions studied in this paper can either be trivial or have been solved [9]–[11]. For a graph G , we denote its maximum degree as $\Delta(G)$. When each node v_i has n_i data items, we define the weighted degree, denoted as $\tilde{d}_{v_i}(G)$, of a node v_i in graph G as $n_i + \sum_{v_j: v_i v_j \in G} n_j$. The maximum weighted degree of a graph G , denoted as $\tilde{\Delta}(G)$, is defined as $\max_i \tilde{d}_{v_i}(G)$.

Each wireless node has an ability to monitor the environment, and collect some data (such as temperature). Assume that there is a subset of n wireless node $V \in U$ that collected some data. $A = \{a_1, a_2, \dots, a_N\}$ is a totally ordered multi-set of N elements collected by all n nodes V . Here, N is the cardinality of set A . Each node v_i has n_i amount of raw data, denoted as $A_i \subset A$. Since A is a multi-set, we assume $A_i \cap A_j = \emptyset$ for $i \neq j$ and $A = \bigcup_{i=1}^n A_i$. Then $\langle A_1, A_2, \dots, A_n \rangle$ is called a distribution of A at sites of V . We assume that one packet (*i.e.*, message) can contain one data item a_i , the node ID, plus additional constant number of bits, *i.e.*, the packet size is at the order of $\Theta(\log n + \log U)$, where U is the upper-bound on values of a_i . Such a restriction on the message size is realistic and needed, otherwise a single

convergecast would suffice to accumulate all data items to the sink which will subsequently solve the problems easily. We consider a TDMA MAC schedule and assume that one time-slot duration allows transmission of exactly one packet.

If energy consumption is to be optimized, we assume that the *minimum* energy consumption by a node u to send data correctly to a node v , denoted as $E(u, v)$, is $c_1 \cdot \|u - v\|^\alpha$, where c_1 (normalized to 1 hereafter) and $\alpha \geq 2$ are constants depending on the environment. We assume that each wireless sensor node can dynamically adjust its transmission power to the minimum needed. We note that in practice, the transmission energy often depending on the power level set by the sensor nodes. Thus, we assume that all nodes will be able to dynamically adjust its transmission power level based on the communication neighboring node. Additionally, for a node v_i to send a data packet to a neighboring node v_j (with $v_i v_j \in G$), node v_j will also spend energy for receiving. In this paper, we assume that the receiving energy cost for a single packet is a fixed value E_r . We first assume that $E_r = 0$.

For data queries in WSNs, we often need build a spanning tree T of the communication graph G first for pushing down queries and propagating back the intermediate results. Given a tree T , let $H(T)$ denote the height of the tree, *i.e.*, the number of links of the longest path from root to all leaf nodes. The depth of a node v_i in T , denoted as $d_T(v_i)$, is the length of the path from the root to v_i . The subtree of T rooted at a node v_i is denoted as $T(v_i)$, the parent node of v_i is denoted as $p_T(v_i)$, and the set of children nodes of a node v_i is denoted as $\text{Child}(v_i)$.

B. Problems and Complexities

We will mainly study the time complexity, message complexity, and energy complexity of data collection in wireless sensor networks.

The complexity measures we use to evaluate the performance of a given protocol are worst-case measures. The *message complexity* (and the *energy complexity*, respectively), of a protocol is defined as the maximum number of total messages (the total energy used, respectively) by all nodes, over all inputs, *i.e.*, over all possible wireless networks \mathcal{G} of n nodes (and possibly with additional requirement of having diameter D and/or maximum nodal degree Δ) and all possible data distributions of A over V . The *time complexity* is defined as the lapsed time from the time when the first message was sent to the time when the last message was received. The *lower bound* on a complexity measure (*e.g.*, message complexity) is the minimum complexity (*e.g.*, message complexity) required by *all* protocols that answer the queries correctly. The approximation ratio ρ_T (resp. ρ_M and ρ_E) for an algorithm denotes the worse ratio of the time complexity (resp. message complexity and energy consumption) used by this algorithm compared to an optimal solution over all possible problem instances.

Here we assume that TDMA MAC is used for channel usage. Obviously, the complexity depends on the TDMA schedule policy \mathcal{S} . Let $X(v_i, t)$ denote whether node v_i will transmit at time slot t or not. Then a TDMA schedule policy \mathcal{S} is to assign 0 or 1 to each variable $X(v_i, t)$. A TDMA

schedule should be *interference free*: no receiving node is within the interference range of the other transmitting node. In other words, if the schedule is define for tree T , for any time slot t , if $X(v_i, t) = 1$, then $X(v_j, t) \neq 1$ for any node v_j such that $p_T(v_i)$ is within the interference range of v_j .

Data collection is an operation to collect the set of *raw* data items A from all sensor nodes to the sink node. It can be done by building a spanning tree T rooted at the sink v_0 , and sending the data at every node v_i to the root node along the unique path in the tree. Clearly, the **message complexity** of data collection along T is $\sum_{i=1}^n n_i \cdot d_T(v_i)$. The **energy complexity**, defined as the total energy needed by all nodes for completing an operation, of data collection using T is $\sum_{i=1}^n [E(v_i, p_T(v_i)) \cdot \sum_{v_j \in T(v_i)} n_j]$.

The TDMA schedule should also be *valid* in the sense that every datum in the network will be relayed to the root. In other words, in tree T , when node v_i sends a datum to its parent $p_T(v_i)$ at a time slot t , node $p_T(v_i)$ should relay this datum at some time-slot $t' > t$. The largest time \mathcal{D} such that there exists a node v_i with $X(v_i, \mathcal{D}) = 1$ is called the **time complexity** of this valid schedule. Time \mathcal{D} is also called the *mark-span* of the schedule \mathcal{S} . Generally, a schedule \mathcal{S} can be defined as assigning 0 or 1 to variable $X(v_i, t, k)$: it is 1 if and only if node v_i will relay datum a_k at time slot t . Clearly, a schedule \mathcal{S} is *valid* for data collection of A using tree T , iff for every node v_i and time slot t ,

$$\sum_{v_j \in \text{Child}(v_i)} \sum_{b=1}^{t-1} X(v_j, b) + n_i \geq \sum_{b=1}^t X(v_i, b).$$

Here $\sum_{v_j \in \text{Child}(v_i)} \sum_{b=1}^{t-1} X(v_j, b) + n_i$ is the total number of data items node v_i has seen so far till time slot t and $\sum_{b=1}^t X(v_i, b)$ is the total number of data items that have been relayed by node v_i so far till time slot t . Then the time-complexity optimizing data collection problem is to find a spanning tree T and a *valid, interference-free* schedule \mathcal{S} such that the mark-span is minimized.

In this paper, we will mainly study the complexity and efficient algorithm for data collection in wireless sensor networks. To address each of these problems, we usually first build a spanning tree T and then decide a interference-free and valid schedule of nodes activities such that certain complexity measure is optimized. However, our lower bound and approximation argument do not depend on the communication graph used, which may not be a tree.

III. CONNECTED DOMINATING SET

A number of our methods will be based on a ‘‘good’’ connected dominating set (CDS) that has bounded degree \mathbf{d} and bounded hop spanning ratio. Here a subgraph H of G is a connected dominating set if (1) graph H is connected, and (2) the set of vertices of H is a *dominating set*, i.e., for every node $v \in G \setminus H$, there is a neighboring node $u \in H$, i.e., $uv \in G$. Notice that in this paper we treat CDS as a graph which includes the edges between dominators and connectors in CDS (as shown in Figure 1(b)). A subgraph H of G has a bounded spanning ratio if for every pair of nodes u and v in H , the distance (hop or weighted distance) of the shortest

path connecting u and v in H is at most a constant times of the distance of the shortest path connecting them in graph G .

A number of methods have been proposed in the literature to construct such a good CDS. See [1], [2] for more details. A simple method is to partition the deployment region into grid of size $r/\sqrt{2}$, select a node (called *dominator*) from each cell if there is any, and then find nodes (called *connectors*) to connect every pair of dominators that are at most 3-hops apart. Then the diameter of the CDS is at most a constant times of the original diameter of graph G . The complexity of building a good CDS at each node is only $O(d \log d)$, where d is the number of neighbors of that node. We assume the availability of a good CDS hereafter.

Given a graph $G = (V, E)$, let $\mathbf{C} = (V_{\mathbf{C}}, E_{\mathbf{C}})$ be a connected dominating set of G where $V_{\mathbf{C}}$ is the set of dominators and connectors and $E_{\mathbf{C}}$ is the edges between dominators and connectors. See Figure 1 for illustration. For a node $v \in V_{\mathbf{C}}$, let $T_{\mathbf{C}}$ be a BFS tree of \mathbf{C} . For a node $v \in V \setminus V_{\mathbf{C}}$, we define a unique dominator $d(v)$ which is the one having the shortest hop distance to the sink v_0 .

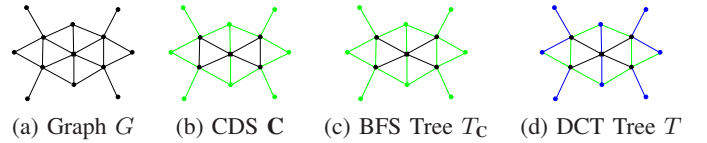


Fig. 1. Illustrations of a graph G , a CDS \mathbf{C} of G , the BFS tree $T_{\mathbf{C}}$, and the data communication tree (DCT) T .

Definition 1 (Data Communication Tree (DCT)): For a graph G and its CDS, the data communication tree T is defined as follows: $T = (V, T_{\mathbf{C}} \cup \{\overline{vd(v)} \mid v \in V \setminus V_{\mathbf{C}}\})$.

Given data communication tree, an aggregate operation (including data collection) consists of (possibly repeated) two phases: a *propagation* phase where the query demands are pushed down into the sensor network along the tree; and an *aggregation* phase where the aggregated values are propagated up from the children to their parents. We discuss some properties of the data communication tree.

Theorem 1: Let G and \mathbf{C} be a graph and its CDS respectively. The data communication tree T has following properties:

- 1) $\Delta(T_{\mathbf{C}}) \leq \mathbf{d}$.
- 2) For any edge $e \in E_T$, let $I(e)$ be the set of edges in $T_{\mathbf{C}}$ that have interferences with e , then $|I(e)| \leq c \cdot \mathbf{d} \cdot \Delta(G)$ for some constant c depending on R/r .

Proof: The first property directly comes from the property of the CDS \mathbf{C} . For any edge $e = \overline{uv} \in E_T$, either u or v will be in \mathbf{C} based on our construction. Assume $u \in V(\mathbf{C})$. For all edges having interferences with e , both end nodes should be within distance $2r + R$ from u . Since $R = \Theta(r)$ and the CDS has a constant-bounded degree, there are at most a constant number of nodes of \mathbf{C} within this range. On the other hand, all edges of T have at least one node in \mathbf{C} . Then it is easy to show that $|I(e)| \leq (\frac{R+2r}{r})^2 \mathbf{d} \cdot \Delta(G)$ by an area argument. ■

All our methods will be based on a good CDS and using **data clustering**: given a good CDS, for a node $v \in V \setminus V_{\mathbf{C}}$, it sends the data items to its dominator $d(v)$ in a TDMA manner.

Lemma 2: Given a good CDS of the graph G , data clustering can be done in time $O(\tilde{\Delta}(G))$.

Proof: We use the communication tree T to do data clustering. For a node $v \in V \setminus V_C$, assume that the edge $vd(v)$ interferes with an edge $ud(u)$. Then dominator nodes $d(u)$ and $d(v)$ are within distance at most $R + 2r$. Thus, there are at most $\frac{(R+2r)^2}{r^2} \mathbf{d}$ such dominator nodes. Thus, the total number of data items of all nodes u such that $ud(u)$ interferes with $vd(v)$ is at most $\frac{(R+2r)^2}{r^2} \mathbf{d} \cdot \tilde{\Delta}(G) = \Theta(\tilde{\Delta}(G))$. Hence, every such edge $vd(v)$ can be scheduled to transmit n_i times in $\Theta(\tilde{\Delta}(G))$ time-slots using a simple greedy coloring method that colors the nodes sequentially using the smallest available color. ■

After data clustering, all data elements are clustered in T_C . In other words, each node v_i in the connected dominating set now will have data from all nodes dominated by v_i . The data clustering asymptotically does not incur additional cost for time complexity and message complexity when $n_i = O(1)$. Notice that the total number of messages for data clustering is $\sum_{v_i \notin V_C} n_i$.

IV. EFFICIENT DATA COLLECTION

In this section, we design efficient methods for collecting data in wireless sensor networks.

A. Minimize Message

We first study the data collection with the minimum number of messages. When all links are reliable, *i.e.*, we only need one message to send a packet from a node u to a node v over a link (u, v) , we should collect any source data from a source node v_i to the sink node v_0 over the path with the minimum number of relay nodes, *i.e.*, with minimum hop number. Thus,

Theorem 3: Data collection can be done with minimum number of messages $\sum_{i=1}^n n_i \cdot h(v_i, v_0)$ using a BFS tree with root v_0 if all links are reliable.

When links are not reliable, let $p(u, v)$ be the reliability of link (u, v) , *i.e.*, with probability $p(u, v)$ the packet will be successfully transmitted over link (u, v) . Assume that the link layer reliability is used. Then clearly, the number of expected transmissions over a link (u, v) is $1/p(u, v)$ for a packet. Thus, to minimize the total relays for sending a packet from its source v_i to the sink node v_0 , the path Π must minimize $\sum_{(u,v) \in \Pi} \frac{1}{p(u,v)}$, which is just the least weighted path from v_i to v_0 when the weight of every link (u, v) is defined as $1/p(u, v)$. Thus, to minimize the messages for data collection, each data packet should be sent using the least weighted path (where the weight of a link (u, v) is $1/p(u, v)$) to the sink node. Let $\mathbf{p}(v_i, v_0)$ be the minimum weight of such shortest path. Let MRPT (maximum reliability path tree) be the tree rooted at v_0 , formed of all these least weighted paths. Thus,

Theorem 4: Data collection can be done with minimum number of messages $\sum_{i=1}^n n_i \cdot \mathbf{p}(v_i, v_0)$ using a MRPT tree with root v_0 if a link (u, v) has a reliability $p(u, v)$.

B. Minimize Energy

We then study the data collection with the minimum energy cost. Apparently, for any element, it should follow the minimum energy cost path from its origin to the sink node v_0 in order to minimize the energy consumption. So minimizing the energy is equivalent to the problem of finding the shortest paths from the sink to all nodes (where the link cost is the its energy cost now), which clearly can be done in time $O(m + n \log n)$ for a communication graph of n nodes and m links. We call the tree formed by minimum energy path from the root to all nodes as the *minimum energy path tree (MEPT)*. Let $\mathbf{E}(v_i, v_0)$ be the energy cost of the path from v_i to v_0 with the minimum energy cost. Thus, we have

Theorem 5: Data collection can be done with minimum energy cost $\sum_{i=1}^n n_i \cdot \mathbf{E}(v_i, v_0)$ using a MEPT tree with root v_0 if a link (u, v) has an energy cost $E(u, v)$.

Clearly, when links are not reliable, we have to take into account the energy cost in retransmissions. In other words, we need use $E(u, v)/p(u, v)$ as the expected energy cost of a link (u, v) . Obviously, the least cost path based routing is also optimum for minimizing the total energy cost of data collection if the receiving energy cost $E_r > 0$.

C. Minimize Time Delay

Then we study the time complexity of data collection. Notice that, the transmissions of nearby nodes should be in different time slots to avoid the interferences. We assume that all links are reliable hereafter.

Algorithm 1 presents our efficient data collection method based on a good CDS \mathbf{C} . The constructed CDS has a degree at most a constant \mathbf{d} , and similar to Theorem 1, all nodes in CDS can be scheduled to transmit once in constant $\beta = \Theta(\mathbf{d})$ time-slots without causing interferences to other nodes in CDS. We take β time-slots as one *round*.

First, the data elements from each dominatee node (a node not in \mathbf{C}) are collected to the corresponding dominator node in the connected dominating set \mathbf{C} . Here the dominatee nodes that are one-hop away from the sink node v_0 will directly send the data to v_0 . Notice that this can be done in time-slots $O(\tilde{\Delta}(G))$ by Lemma 2.

Now we only consider the dominator nodes and the breadth-first-search spanning tree T_C of nodes in CDS rooted at the sink v_0 . Every edge in the tree T_C will be scheduled exactly once in each round. For simplicity, we do not schedule sending an element more than once in the same round. At every round, nodes in CDS push one data item to its parent node until all data are received by v_0 .

Algorithm 1 Efficient Data Collection Using CDS

Input: A CDS \mathbf{C} with bounded degree \mathbf{d} , tree T_C .

- 1: Every node v_i sends its data to its dominator node $d(v_i)$.
 - 2: **for** $t = 1$ to N **do**
 - 3: **for** each node $v_i \in V_C$ **do**
 - 4: If node v_i has data not forwarded to its parent node in T_C , node v_i sends a new data to its parent in round t .
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Theorem 6: Given a connected wireless network G , data collection can be done in time $\Theta(N)$ with $\Theta(\sum_{i=1}^n n_i h(v_i, v_0))$ messages.

Proof: From Lemma 2, in $O(\tilde{\Delta}(G))$ time-slots, the data elements from each dominatee node are collected to the corresponding dominator node in the connected dominating set. We show that after $N + H(T_C)$ rounds, all elements can be scheduled to arrive in the root, where $H(T_C)$ is the height of the BFS tree T_C . Algorithm 1 illustrates our method to achieve this.

A CDS node v is in level i if the path from v to v_0 in BFS tree T_C has i hops. A level i is said to be *occupied* at a time instance if there exists one CDS node from level i that has at least one data. Assume that originally all levels $i \in [1, H(T_C)]$ are occupied, after collecting data from all dominatee nodes. We will show that each round the root will get at least one data item if there are data in the network. We essentially will show that the occupied levels are *continuous*, i.e., before each round t , there is L_t such that all levels in $[1, L_t]$ are occupied and levels in $[L_t + 1, H(T_C)]$ are not. We prove this by induction. This is clearly true for round 1. Assume that it is true for round t . Then in round t , for each level $i \in [1, L_t - 1]$, every node in level $i + 1$ will send its data to its parent in level i . Then every level $i \in [1, L_t - 1]$ will have data for sure before round $t + 1$. Then clearly, $L_{t+1} = L_t$ if some nodes in level L_t still have some data; otherwise we set $L_{t+1} = L_t - 1$. Consequently, root will get at least one data item for each round whenever there are data in the network. Since there are at most N data items, Algorithm 1 will take at most N rounds, i.e., $O(N)$ time-slots because each round is composed of constant β time-slots.

When not all levels are occupied initially, then it is easy to show that after at most $H(T_C)$ rounds, the occupied levels will be *continuous*. Hence, the collection can be done in at most $N + H(T_C)$ rounds. Notice that $H(T_C) = \Theta(D(G))$. Consequently, the total time-slots are at most $O(\tilde{\Delta}(G)) + O(N + D) = O(N)$ since $\tilde{\Delta}(G) \leq N$.

On the other hand, for any data collection algorithm, it needs at least N time slots since the sink can only receive one data item in one time slot and there are N data items.

The total number of messages used by the algorithm is of course at most $4 \sum_{i=1}^n n_i h(v_i, v_0)$ as the element at node v_i are relayed by at most $4 \times h(v_i, v_0)$ nodes in CDS (since $h(v_i, v_0) \geq 2$). Obviously any algorithm needs at least $\sum_{i=1}^n n_i h(v_i, v_0)$ messages. This finishes the proof. ■

V. COMPLEXITY TRADEOFFS FOR DATA COLLECTION

One may want to design a universal data collection method whose time-complexity, message-complexity and energy-complexity are all within constant factors of the optimum. Observe that Algorithm 1 is a constant approximation for both time-complexity and message-complexity. However, it is not a constant approximation for energy-complexity. Consider the following line network example: $n + 1$ nodes are uniformly distributed in a line segment $[0, r]$; Sink v_0 is the leftmost node and node v_i is at position $i \cdot r/n$ and has one data item. Here we assume $r = 1$. See Figure 2 for illustration. Assume the energy cost for a link uv is $\|uv\|^2$. Then the minimum cost

data collection is to let node v_i send all its data to node v_{i-1} . The total energy cost is $\sum_{i=1}^n i \cdot \frac{1}{n^2} \simeq 1/2$. While the energy cost of collecting data via CDS is $\sum_{i=1}^n (\frac{i}{n})^2 \simeq n/6$. On the other hand, the total number of messages of the minimum-energy data collection scheme is $n(n-1)/2$ and the time slots used by this scheme is also $\Theta(n^2)$; both of which are $\Theta(n)$ times of the corresponding minimum.

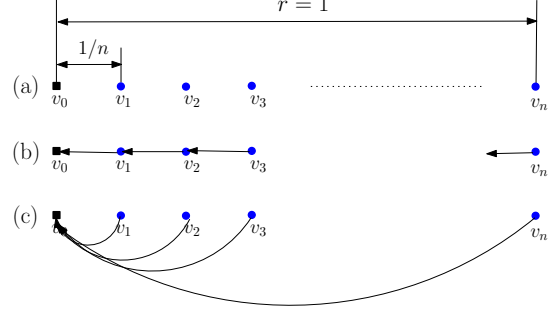


Fig. 2. Example: (a) a line network with $n + 1$ nodes; (b) the minimum energy data collection tree; (c) the data collection tree via CDS, where v_0 is the only dominator.

Consider any data collecting algorithm \mathcal{A} . Let ϱ_M and ϱ_E be the approximation ratio for the message-complexity and energy-complexity of algorithm \mathcal{A} . We show that there are graphs of n nodes such that $\varrho_M \cdot \varrho_E = \Omega(n)$.

Lemma 7: Assume the energy cost for supporting a link uv is $\|uv\|^2$. For any data collection algorithm \mathcal{A} , there are graphs of n nodes, such that $\varrho_M \cdot \varrho_E = \Omega(n)$.

Proof: Consider the line graph example defined previously. For a node v_i , assume that the data collection path is composed of k_i hops and the length of the k_i links are $x_{i,1}, x_{i,2}, \dots, x_{i,k_i}$. Then $\sum_{j=1}^{k_i} x_{i,j} = \frac{i}{n}$. The total energy cost, denoted as e_i , of such data collection path is $e_i = \sum_{j=1}^{k_i} x_{i,j}^2 \geq \frac{(\sum_{j=1}^{k_i} x_{i,j})^2}{k_i}$. Thus,

$$e_i \cdot k_i \geq \left(\frac{i}{n}\right)^2.$$

Obviously, the total number of messages are $\sum_{i=1}^n k_i$ and the total energy cost is $\sum_{i=1}^n e_i$. We will use the Holder's inequality: for positive a_i and b_i , $p > 0$, $q > 0$ with $\frac{1}{p} + \frac{1}{q} = 1$, we have

$$\left(\sum_{i=1}^n a_i^p\right)^{\frac{1}{p}} \left(\sum_{i=1}^n b_i^q\right)^{\frac{1}{q}} \geq \sum_{i=1}^n a_i \cdot b_i.$$

Equivalently, $\left(\sum_{i=1}^n a_i\right)^{\frac{1}{p}} \left(\sum_{i=1}^n b_i\right)^{\frac{1}{q}} \geq \sum_{i=1}^n a_i^{\frac{1}{p}} \cdot b_i^{\frac{1}{q}}$. Then $\left(\sum_{i=1}^n k_i\right) \left(\sum_{i=1}^n e_i\right) \geq \left(\sum_{i=1}^n \sqrt{e_i} \cdot \sqrt{k_i}\right)^2 \geq \left(\sum_{i=1}^n \frac{i}{n}\right)^2 = \frac{(n-1)^2}{4}$. Clearly, the minimum number of messages is n for any scheme and the minimum energy cost is $1/2$ for any scheme. Thus, we have $\varrho_M \cdot \varrho_E \geq (n-1)^2/(2n) = \Theta(n)$. This finishes the proof. ■

Notice that we generally assumed that the energy cost for supporting a link uv is $\|uv\|^\alpha$. Then we can show that

$$(\varrho_M)^{\alpha-1} \varrho_E \geq \frac{n^{\alpha-1}}{2^{\alpha-1}}.$$

Notice that since $\varrho_E \geq 1$ and $\alpha \geq 2$, we have $(\varrho_M)^{\alpha-1}(\varrho_E)^{\alpha-1} \geq (\varrho_M)^{\alpha-1}\varrho_E \geq \frac{n^{\alpha-1}}{2^{\alpha-1}}$. Consequently, $\varrho_M \cdot \varrho_E \geq n/2$ still holds.

When we also take the maximum degree Δ into account, the above lemma implies the following corollary (the proof is essentially same).

Corollary 8: For any data collection algorithm \mathcal{A} , there are graphs of n nodes with maximum degree Δ , such that $\varrho_M \cdot \varrho_E = \Omega(\Delta)$.

The above lemma also implies that for any data collection algorithm \mathcal{A} , $\varrho_M \cdot \varrho_E \cdot \varrho_T = \Omega(\Delta)$, where ϱ_T is the approximation on the time-complexity by algorithm \mathcal{A} . We then show that for Algorithm 1, $\varrho_E = O(\Delta(G))$.

Lemma 9: Algorithm 1 is $\varrho_E = O(\Delta(G))$ -approximation for energy cost.

Proof: Consider any node v_i and its minimum energy path $P_{v_i v_0}(G) = u_1 u_2 \cdots u_k$ to the sink node v_0 in the original communication graph G , where $u_1 = v_i$ and $u_k = v_0$. Assume that the total Euclidean length of this path is h . Obviously, $k \leq h \cdot \Delta/r$ since any node can have at most Δ neighbors within distance r . Let $x_i = \|u_i u_{i+1}\|$. Then the total energy cost is $\sum_{i=1}^{k-1} x_i^2$. Obviously, $\sum_{i=1}^{k-1} x_i^2 \geq \frac{(\sum_{i=1}^{k-1} x_i)^2}{k-1} \geq \frac{h^2 \cdot r}{h\Delta}$. On the other hand, since the Euclidean distance of the shortest path in G between v_i and v_0 is at most h , the shortest hop path connecting them is at most $2\lceil h/r \rceil$ hops. Thus, we can find a path using CDS to connect v_i and v_0 using at most $2 + 3 \cdot \lceil 2h/r \rceil \leq 4\lceil \frac{2h}{r} \rceil$ hops. The inequality is due to $\lceil h/r \rceil \geq 2$. Consequently, the total energy of the path connecting v_i and v_0 based on CDS is at most $4\lceil \frac{2h}{r} \rceil \cdot r^2$. Observe that our data collection algorithm based on CDS will use the shortest hop path to route the data from v_i to the sink v_0 . Thus, the energy cost of data collection using CDS is at most $\Theta(\Delta)$ times of the minimum. This finishes the proof. ■

Consequently, we know that Algorithm 1 is asymptotically optimum if we want to optimize the time-complexity, message-complexity and energy-cost-complexity simultaneously. On the other hand, the minimum energy data-collection based on minimum energy path tree (MEPT) has delay that is at most $O(\Delta^4)$ times of the optimum.

Lemma 10: Data collection using MEPT is $\varrho_E = O(\Delta(G)^4)$ -approximation for time complexity.

Proof: Consider the node v such that its minimum energy path P to the root has maximum number of hops, which contains data. Assume P has h hops with Euclidean length y_1, y_2, \dots, y_h . Then $\sum_{i=1}^h y_i \geq \frac{hr}{\Delta}$ since every node can have at most Δ nodes within r distance. The total energy of this path is $\sum_{i=1}^h y_i^2 \geq \frac{(\sum_{i=1}^h y_i)^2}{h} \geq \frac{hr^2}{\Delta^2}$. On the other hand, consider the path from v to root with minimum number of hops h_2 . For this path, its energy cost is at most $h_2 r^2$, which should be at least $\sum_{i=1}^h y_i^2$ due to optimality of P . Thus, $h_2 r^2 \geq \frac{hr^2}{\Delta^2}$ implies that $h \leq h_2 \Delta^2$.

Now consider an edge in the MEPT, scheduling this edge will interfere $O(\Delta^2)$ nodes. Since MEPT is planar, at most $O(\Delta^2)$ edges in MEPT will be interfered. In other words, if we take one round to be $O(\Delta^2)$ time slots, each edge in the MEPT can be scheduled once. The height of the MEPT to be h . Scheduling the MEPT in a fashion similar to Algorithm 1

can finish the data collection operation in $O(N + h)$ rounds, hence $O(\Delta^2(N + h))$ time slots. On the other hand, any data collection algorithm will take $\Omega(N + h_2)$ time slot. Hence, data collection using MEPT is $\varrho_E = O(\Delta(G)^4)$. ■

We construct a network example, in which the MEPT has delay that is $\Omega(\Delta^2)$ times of the optimum. Consider a rectangle $uvwz$ with side-length $\|uv\| = p \cdot r$ and $\|uz\| = p \frac{\Delta-2}{8} r(1-\epsilon)$. There are $p+1$ nodes $u = u_1, u_2, \dots, u_{p+1} = v$ uniformly distributed over the segment uv and $q = p\Delta^2/8 - 1$ nodes v_1, v_2, \dots, v_q uniformly distributed over the rest of the 3 segments. Then it is easy to show that the MEPT path connecting u and v is $uv_1 v_2 \cdots v_q v$, with $q = p\Delta^2/8 - 1$ hops. Obviously, the path $u_1 u_2 \cdots u_p$ connecting u and v has the least delay p .

VI. DATA AGGREGATION

We consider the case when the data aggregation is distributive. In other words, given any node v and its set of children nodes u_1, u_2, \dots, u_d , where d is the number of children nodes of v in a data aggregation tree, the data produced by node v has size same as the size of each of the individual node. Typical examples of such aggregation are *min*, *max*, *average*, or *variance*. In data aggregation, if one node send information twice, it can always save the first transmission. Hence, the data aggregation should be done using a tree.

A. Message, Energy, and Time Complexity

Message Complexity: The total message complexity for data aggregation using any tree T is $\Theta(n)$, where n is the number of nodes of the network. The lower bound on the message complexity n is obvious since every node v needs send at least once. The upper bound is also n because we can do the data aggregation using any spanning tree and every node only needs to send once.

Energy Complexity: For distributive aggregation, it seems that we need use some data aggregation tree that is energy efficient since each node needs to send at least once. So the main question now is to construct a tree such that the total cost of all links are minimized. This clearly is the minimum spanning tree, where the link cost of any link uv is the energy cost of sending a unit amount of data over the link uv , which can be computed in polynomial time.

Time Complexity: We will show that the time complexity for such kind of data aggregation is of the order $\Theta(H + \Delta(G))$, where H is the height of the BFS tree rooted at the sink node v_0 . Notice that for a BFS tree for a graph G , its height H is $\Theta(D(G))$, thus the time complexity is of the order of $\Theta(D + \Delta(G))$ too. Algorithm 2 illustrates our method.

Theorem 11: Data aggregation can be done in $\Theta(D + \Delta)$ time with n messages.

Proof: The lower bound on the time complexity is obvious since for the node v that is farthest (with the largest hop distance) from the root, it needs at least H time slots to reach the root. Additionally, it obviously needs at least $\Delta(G)$ time-slots to schedule all nodes' transmissions due to interference constraints.

Algorithm 2 Efficient Data Aggregation Using CDS

Input: A CDS \mathbf{C} with bounded degree \mathbf{d} , a distributive function f and corresponding function h .

- 1: **for** each dominator node v_i **do**
 - 2: For the set of dominatee nodes of the node v_i , we build a minimum spanning tree (MST) rooted at v_i , where the link weight is the energy cost for supporting the link communication. The data elements from all these dominatee nodes are then *aggregated* to the corresponding dominator node v_i along the minimum spanning tree of these dominatee nodes. In other words, any node v_k will compute $h(f(A_k), x_{k,1}, x_{k,2}, \dots, x_{k,d_k})$ where $x_{k,j}$, for $j \in [1, d_k]$, is the aggregated value node v_k received from its j th child in the minimum spanning tree and d_k is the number of children of node v_k in the MST of all dominatee nodes of v_i . Notice that this aggregation can be done in time-slots $\Theta(\Delta(G))$.
 - 3: Now we only consider the dominator nodes and the breadth-first-search spanning tree T_C of nodes in CDS rooted at the sink v_0 .
 - 4: **for** $t = 1$ to H **do**
 - 5: **for** each node $v_i \in V_C$ **do**
 - 6: If node v_i has received aggregated data from all its children nodes in T_C , it sends the aggregated data (using its own data and all aggregated data from its children) to its parent node in round t .
-

We then show that Algorithm 2 takes time $\Theta(H + \Delta(G))$. The first step that let each dominatee node send its data to its dominator node will take time-slots at most $\Theta(\Delta(G))$. Then we perform aggregation in round, where each round is composed of β time slots (where constant β is the number of colors needed to color the interference graph induced by all CDS nodes). In round 1, all nodes in level H (all leaves) send a message to their parents. In round t , all nodes in level $H - t + 1$ should have received all the messages from their children, compute the aggregation of all data received so far, and then send the aggregated values to their parents. In all, the total number of rounds to finish data aggregation is H . Recall that each round is composed of β time-slots. Thus, Algorithm 2 takes time $\Theta(H + \Delta(G))$. Since, $H = \Theta(D)$, this finishes the proof. ■

If there are more than one aggregation functions, we can deliver the messages one by one. We call this as sequential aggregation.

Corollary 12: k sequential data aggregations can be done in $O(D + \Delta + k)$ time with kn messages.

B. Complexity Tradeoffs

Again, we may want to design a data aggregation method that has constant approximation ratios for message complexity, time complexity, and energy complexity. First, aggregation based on MST (that is energy optimum for aggregation) is not efficient for time complexity.

Lemma 13: The minimum energy data aggregation based on MST is $\varrho_T = \Omega(\min(\frac{n}{\Delta}, \sqrt{n\Delta}))$ -approximation for time

complexity. On the other hand, $\varrho_T = O(\frac{n}{\Delta})$.

Proof: Consider a set of wireless nodes in a grid, with size length r' . Then $\Delta = \Theta((1/r')^2)$ and $D = \Theta(\sqrt{nr'}) = \sqrt{n/\Delta}$, assuming the communication range to be 1. There exists a MST T which consists of n sequential line segments. See Figure 3 for an example. In fact, we can perturb the grid slightly, so that this bad MST is the only MST on the grid.

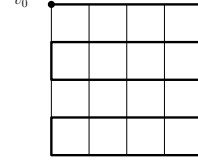


Fig. 3. Example of a bad MST.

Clearly, the data aggregation on T takes $\Theta(n)$ time slots. On the other hand, Algorithm 2 takes $O(\Delta + D)$ time slots. Notice that the diameter of the CDS is a constant factor of the original graph. Hence, $\varrho_T \geq \Omega(\frac{n}{\Delta + D}) = \Omega(\frac{n}{\Delta + \sqrt{n/\Delta}})$. The lower bound follows by considering the cases that $n \geq \Delta^3$ and $n \leq \Delta^3$.

Now consider the upper bound, the data aggregation on a MST takes at most $n - 1$ time slots. However, any optimal solution should take $\Omega(\Delta + D)$. Hence $\varrho_T = O(n/\Delta)$. ■

Observe that our method (Algorithm 2) has constant ratio for both message complexity and time complexity. However, it is not always energy efficient due to the following lemma.

Lemma 14: Algorithm 2 is $\varrho_E = O(\Delta(G))$ -approximation for energy cost.

Proof: First, consider any dominator u and let v_1, v_2, \dots, v_d be the d dominatee nodes associated with u , where $d \leq \Delta$, and $\|v_i u\| \leq r$. Let x_1, x_2, \dots, x_d be the d edges of the minimum spanning tree connecting u and its associated dominatees. It was proved in [?] that

$$\sum_{i=1}^d x_i^2 \leq 6r^2.$$

Assume that there n_d dominator nodes in CDS (e.g., we can use a maximal independent set as a dominating set). Obviously, $n_d \cdot \Delta \geq n$. Then the total energy cost of aggregating data from all dominatee nodes to dominators is at most $6n_d r^2$. Recall that in our CDS, all nodes in V_C will have at most \mathbf{d} neighbors. It is easy to show that the total energy cost of aggregating data over CDS is at most $\mathbf{d} \cdot n_d \cdot r^2$. Thus, the total energy cost of aggregating data using Algorithm 2 is at most $(\mathbf{d} + 6) \cdot n_d \cdot r^2 = \Theta(n_d \cdot r^2)$.

We then study the minimum cost of data aggregation, which is to use the minimum spanning tree of original communication graph G . Let y_1, y_2, \dots, y_n be the length of the n edges of the MST connecting $n+1$ nodes v_0, v_1, \dots, v_n . Since there are n_d independent nodes, it is easy to show that the MST will have length at least $n_d \cdot r$, i.e., $\sum_{i=1}^n y_i \geq n_d r$. The total energy cost of data aggregation based on minimum spanning tree is $\sum_{i=1}^n y_i^2$. Notice, $\sum_{i=1}^n y_i^2 \geq (\sum_{i=1}^n y_i)^2 / n \geq n_d^2 r^2 / n$.

Then our algorithm has approximation ratio on energy cost at most $\frac{(\mathbf{d}+6) \cdot n_d \cdot r^2}{\frac{n_d^2 r^2}{n}} \leq (\mathbf{d} + 6)\Delta = O(\Delta)$, because of $n_d \cdot \Delta \geq$

n .

We then show that there are examples of networks (with maximum degree Δ) such that Algorithm 2 is $\varrho_E = \Theta(\Delta(G))$ -approximation for energy cost. Consider a line graph composed of $n + 1$ nodes evenly distributed in a segment $[0, \frac{2r}{\Delta}n]$, i.e., node v_i is at position $\frac{2r}{\Delta} \cdot i$, for $i \in [0, n]$. See Figure 4 for illustration. It is easy to show that the minimum energy data aggregation tree is simply the path $v_0v_1 \cdots v_{n-1}v_n$, whose total energy cost is $n(\frac{2r}{\Delta})^2$. On the other hand, the energy cost of using tree T_C is $\Theta(\frac{2n}{\Delta}r^2)$ since the CDS will have $\frac{2n}{\Delta}$ nodes. The energy cost using tree T_C is $\Theta(\Delta)$ times of the minimum. This finishes the proof. ■

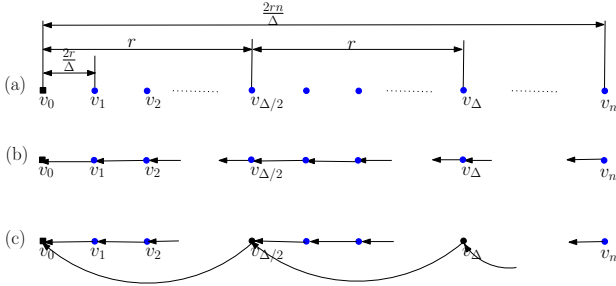


Fig. 4. Example: (a) the line network with $n + 1$ nodes; (b) the minimum energy data aggregation tree; (c) the tree T_C .

Although our method is not energy efficient in the worst case (with approximation ratio up to $\Theta(\Delta)$ in the worst case), we show that it is the best we can do if we want to achieve $\Theta(1)$ ratio in delay. Again, given a data aggregation method \mathcal{A} , let ϱ_E , ϱ_T and ϱ_M be the approximation ratios of \mathcal{A} over all networks with n nodes and maximum degree Δ . We prove the following lemma.

Lemma 15: For any data aggregation algorithm \mathcal{A} , there are graphs of n nodes with maximum degree Δ , such that $\varrho_T \cdot \varrho_E = \Omega(\Delta)$.

Proof: Again consider the line network example used in the proof of Lemma 14. Assume that we choose a tree T for data aggregation. Consider the unique path P from v_0 to v_n in T . Assume P has k edges. Then the data aggregation using T takes at least k time slots. Let $\{x_i\}$ be the Euclidean lengths of the k edges in P . Clearly, $\sum_1^k x_i \geq 2rn/\Delta$. Then, the energy cost of this path is $\sum_1^k x_i^2 \geq (\sum_1^k x_i)^2/k \geq 4r^2n^2/(k\Delta^2)$. Notice that for any algorithm, the minimum delay is $2n/\Delta$ (using CDS) and the minimum energy cost is $4nr^2/\Delta^2$ (using MST). Thus, the approximation ratio ϱ_T and ϱ_E satisfy that:

$$\varrho_T \cdot \varrho_E \geq \frac{k}{\frac{2n}{\Delta}} \cdot \frac{\frac{4nr^2}{\Delta^2}}{\frac{4r^2n^2}{k\Delta^2}} = \frac{\Delta}{2}. \quad \blacksquare$$

C. Minimizing the maximum energy consumption by a node

In many applications, we may need to reduce the maximum energy consumption by all nodes, instead of minimizing the total energy consumption by all nodes for data aggregation. We assume that all nodes have the same amount of data to be aggregated and the aggregation function f satisfies that $f(a_1, a_2, \dots, a_p)$ has size as the maximum size of a_i , i.e., the aggregated data can be represented by a single packet if each of the input data items is represented by a single packet. In

this subsection, we then study how to design efficient method for minimizing the maximum energy consumption for data aggregation. We first assume that the energy consumption for sending a single data packet over all links $v_iv_j \in G$ is the same (say E) or within a small constant factor μ of each other (i.e., $E(v_iv_j) \leq \mu E(v_p, v_q)$ for all links v_iv_j and v_pv_q). Observe that this is often the case in practice. We also assume that every node has P original data packets to be aggregated. For a data aggregation tree T and an internal node v_i , the energy cost is $(E_r \cdot d_{v_i}(T) + E) \cdot P$, where E_r is the energy cost for receiving a data packet, and E is the energy cost for sending a packet. To minimize the maximum energy cost of nodes v_i in T , it is equivalent to minimize $d_{v_i}(T)$, i.e., the maximum node degree of T . Then it is easy to show the following lemma.

Lemma 16: Minimizing the maximum energy consumption by all nodes for data aggregation is equivalent of finding a spanning tree T with the minimum maximum node degree in T .

Finding a spanning tree T in a general graph with minimum degree is NP-hard problem. Recently, Blin *et al.* [4] proposed a distributed method that can find a spanning tree with maximum node degree at most $OPTree(G) + 1$, where $OPTree(G)$ is the smallest maximum node degree of all spanning trees for G . In this paper, we assumed that only a subset $V \subseteq U$ of nodes have data to be aggregated. Thus, we need a Steiner tree T that minimizes the maximum node degree if a single spanning tree T is needed for data aggregation. A polynomial time algorithm that produces a Steiner tree T (spanning a subset V of nodes in a general graph G) with the maximum degree at most $OPTree(G, V) + 1$ is presented in [7]. This implies the following lemma.

Lemma 17: If a single data aggregation tree T is required for aggregating data items from a subset V of sensor nodes, we can construct a tree T in polynomial time such that the maximum energy consumed by any node in T is at most $\mu \cdot (1 + \frac{1}{OPTree(G, V)})$ times of the optimum.

In addition to only minimizing the maximum energy cost by a node, in practice, we often need to minimize the total energy cost while the maximum energy cost by a node v_i is at most a value $E_s(v_i)$. We first show that this problem is NP-hard. Notice that for a data aggregation tree T , and a node v_i in T we know that the energy cost of node v_i is $E_r \cdot d_{v_i}(T) + E$ when we need aggregate a single packet from each of the nodes in V . Then requiring that the total energy cost of node v_i is at most a value $E_s(v_i)$ is equivalent as $E_r \cdot d_{v_i}(T) + E \leq E_s(v_i)$, i.e., the node degree of v_i in T , $d_{v_i}(T) \leq \frac{E_s(v_i) - E}{E_r}$. Thus, an upper bound on energy consumption is equivalent as specifying an upper bound $B(v_i) = \frac{E_s(v_i) - E}{E_r}$ on the node degree of v_i in the spanning tree. Then for all spanning trees meeting this degree requirement for all nodes $v_i \in V$, we will find a spanning tree with the minimum total energy cost. Given a wireless network G , and a degree requirement specified by a vector B , let $MCost(G, B)$ be the minimum cost of all the spanning trees in G that satisfy the degree requirement B . Based on a recent result by [16], we can prove the following theorem.

Theorem 18: Given a degree upper bound $B(v_i)$ for each node v_i , there is a polynomial time algorithm that can find a data aggregation tree T such that the degree $d_{v_i}(T)$ of node

v_i in T satisfies that $d_{v_i}(T) \leq B(v_i) + 1$, and the energy cost of T is at most $MCost(G, B)$.

VII. RELATED WORK

Most existing convergecast methods [3], [8], [17] are based on a tree structure and with minimum either energy or data latency as the objective. For example, [17] first constructs a tree using greedy approach and then allocates DSSS or FHSS codes for its nodes to achieve collision-free, while [3], [8] uses TDMA to avoid collisions. In [3], the authors did *not* give any theoretical tradeoffs between energy cost and latency. Zhang and Huang [19] proposed a hop-distance based temporal coordination heuristic for adding transmission delays to avoid collisions. They studied the effectiveness of packet aggregation and duplication mechanisms with such convergecast framework. Kennelman and Kowalski [11] proposed a randomized distributed algorithm for convergecast that has the expected running time $O(\log n)$ and uses $O(n \log n)$ times of minimum energy in the worst case, where n is the number of nodes. They also showed the lower bound of running time of any algorithm in an arbitrary network is $\Omega(\log n)$. However, they assume that all nodes can dynamically adjust its transmission power from 0 to any arbitrary value and a data message by a node can contain *all* data it has collected from other nodes. In [5], Chu *et al.* studied how to provide approximate and bounded-loss data collection in sensor networks instead of accurate data. Their method used replicated dynamic probabilistic models to minimize communication from sensor nodes to the base station.

To significantly reduce communication cost in sensor networks, in-network aggregation has been studied and implemented. In TAG (Tiny AGgregation service) [12], besides the basic aggregation types (such as *count*, *min*, *max*, *sum*, *average*) provided by SQL, five groups of possible sensor aggregates are summarized: distributive aggregates (*e.g.*, *count*, *min*, *max*, *sum*), algebraic aggregates (*e.g.*, *average*), holistic aggregates (*e.g.*, *median*), unique aggregates (*e.g.*, *count distinct*), and content-sensitive aggregates (*e.g.*, *fixed-width histograms* and *wavelets*). Notice that the first two groups aggregates are very easy to achieve by a tree-based method. To overcome the severe robustness problems of the tree approaches [12], [13], [18], multipath routing for in-network aggregation has been proposed [6], [15]. Then recently Manjhi *et al.* [14] combined the advantages of the tree and multi-path approaches by running them simultaneously in different regions of the network. In [9], Kashyap *et al.* studied a randomized (gossip-based) scheme using which all the nodes in a complete overlay network can compute the common aggregates of *min*, *max*, *sum*, *average*, and *rank* of their values using $O(n \log \log n)$ messages within $O(\log n \log \log n)$ rounds of communication. Kempe *et al.* [10] earlier presented a gossip-based method which can get the average in $O(\log n)$ rounds with $O(n \log n)$ messages.

VIII. CONCLUSION

In this paper, we study the time complexity, message complexity, and energy complexity of data collection in wireless

sensor networks. We first present efficient algorithms that achieve asymptotically optimal message complexity, energy complexity, and time complexity. We then study the lower bound of the complexities for these problems and show that our method achieves the best possible tradeoffs among these three metrics. There are still a number of interesting questions left for future research. One is to design efficient algorithms when each node will produce a data stream. The second challenge is what is the best algorithm when we do not require that the found data item to be precise, *i.e.*, we allow certain relative errors, or additive errors on the found answer. We also need to study the lower bound on energy cost and design energy efficient algorithm for other data operations, such as aggregation, selection, top- k query, and other holistic queries such as *most frequent items*, *number of distinctive items*.

IX. ACKNOWLEDGEMENT

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REFERENCES

- [1] ALZOUBI, K., LI, X.-Y., WANG, Y., WAN, P.-J., AND FRIEDER, O. Geometric spanners for wireless ad hoc networks. *IEEE Transactions on Parallel and Distributed Processing* 14, 4 (2003), 408–421. Short version in IEEE ICDCS 2002.
- [2] ALZOUBI, K. M., WAN, P.-J., AND FRIEDER, O. Message-optimal connected dominating sets in mobile ad hoc networks. In *Proceedings of the 3rd ACM international symposium on Mobile ad hoc networking & computing* (2002), ACM Press, pp. 157–164.
- [3] ARUMUGAM, M., AND KULKARNI, S. S. Tradeoff between energy and latency for convergecast. In *Proceedings of the Second International Workshop on Networked Sensing Systems (INSS)* (2005).
- [4] BLIN, L., AND BUTELLE, F. The first approximated distributed algorithm for the minimum degree spanning tree problem on general graphs. In *Parallel and Distributed Processing Symposium, 2003. Proceedings. International* (2003), p. 6.
- [5] CHU, D., DESHPANDE, A., HELLERSTEIN, J. M., AND HONG, W. Approximate data collection in sensor networks using probabilistic models. In *ICDE '06: Proceedings of the 22nd International Conference on Data Engineering (ICDE'06)* (Washington, DC, USA, 2006), IEEE Computer Society, p. 48.
- [6] CONSIDINE, J., LI, F., KOLLIOS, G., AND BYERS, J. Approximate aggregation techniques for sensor databases. In *ICDE '04: Proceedings of the 20th International Conference on Data Engineering* (Washington, DC, USA, 2004), IEEE Computer Society, p. 449.
- [7] FÜRER, M., AND RAGHAVACHARI, B. Approximating the minimum-degree steiner tree to within one of optimal. In *SODA: selected papers from the third annual ACM-SIAM symposium on Discrete algorithms* (Orlando, FL, USA, 1994), Academic Press, Inc., pp. 409–423.
- [8] GANDHAM, S., ZHANG, Y., AND HUANG, Q. Distributed minimal time convergecast scheduling in wireless sensor networks. In *ICDCS '06: Proceedings of the 26th IEEE International Conference on Distributed Computing Systems* (Washington, DC, USA, 2006), IEEE Computer Society, p. 50.
- [9] KASHYAP, S., DEB, S., NAIDU, K. V. M., RASTOGI, R., AND SRINIVASAN, A. Efficient gossip-based aggregate computation. In *PODS '06: Proceedings of the twenty-fifth ACM SIGMOD-SIGACT-SIGART symposium on Principles of database systems* (New York, NY, USA, 2006), ACM, pp. 308–317.

- [10] KEMPE, D., DOBRA, A., AND GEHRKE, J. Gossip-based computation of aggregate information. In *FOCS '03: Proceedings of the 44th Annual IEEE Symposium on Foundations of Computer Science* (Washington, DC, USA, 2003), IEEE Computer Society, p. 482.
- [11] KESSELMAN, A., AND KOWALSKI, D. R. Fast distributed algorithm for convergecast in ad hoc geometric radio networks. *J. Parallel Distrib. Comput.* 66, 4 (2006), 578–585.
- [12] MADDEN, S., FRANKLIN, M. J., HELLERSTEIN, J. M., AND HONG, W. TAG: A Tiny AGgregation service for ad-hoc sensor networks. In *Proc. 5th USENIX OSDI* (Boston, MA, Dec. 2002).
- [13] MADDEN, S., FRANKLIN, M. J., HELLERSTEIN, J. M., AND HONG, W. The design of an acquisitional query processor for sensor networks. In *SIGMOD '03: Proceedings of the 2003 ACM SIGMOD international conference on Management of data* (New York, NY, USA, 2003), ACM, pp. 491–502.
- [14] MANJHI, A., NATH, S., AND GIBBONS, P. B. Tributaries and deltas: efficient and robust aggregation in sensor network streams. In *SIGMOD '05: Proceedings of the 2005 ACM SIGMOD international conference on Management of data* (New York, NY, USA, 2005), ACM, pp. 287–298.
- [15] NATH, S., GIBBONS, P. B., SESHAN, S., AND ANDERSON, Z. R. Synopsis diffusion for robust aggregation in sensor networks. In *SenSys '04: Proceedings of the 2nd international conference on Embedded networked sensor systems* (New York, NY, USA, 2004), ACM, pp. 250–262.
- [16] SINGH, M., AND LAU, L. Approximating minimum bounded degree spanning trees to within one of optimal. In *Proceedings of the thirty-ninth annual ACM symposium on Theory of computing* (2007), ACM New York, NY, USA, pp. 661–670.
- [17] UPADHYAYULA, S., ANNAMALAI, V., AND GUPTA, S. A low-latency and energy-efficient algorithm for convergecast in wireless sensor networks. In *IEEE GLOBECOM: Global Telecommunications Conference* (2003), vol. 6, pp. 3525–3530.
- [18] YAO, Y., AND GEHRKE, J. Query processing in sensor networks. In *Proc. of Conference on Innovative Data System (CIDR)* (2003).
- [19] ZHANG, Y., AND HUANG, Q. Coordinated Convergecast in Wireless Sensor Networks. *Military Communications Conference, 2005. MILCOM 2005. IEEE* (2005), 1–7.